

# Papers in Computational Methods for $D$ -modules

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This is a collection of papers in computational  $D$ -module theory. The scope is limited to computation of invariants of  $D$ -modules including functors of homology algebra in  $D$ -modules. If there are papers which are not cited, please let me know them.

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